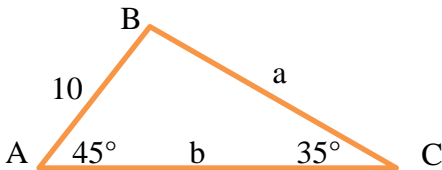
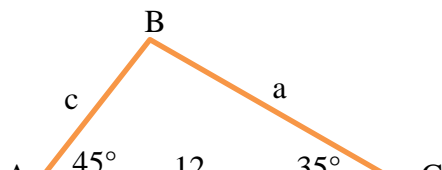
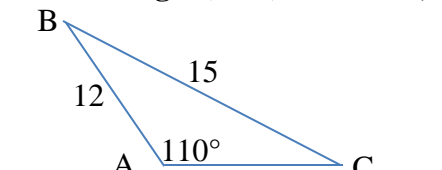
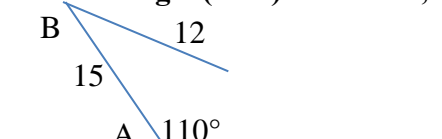
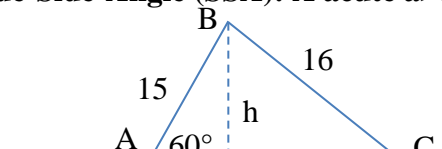
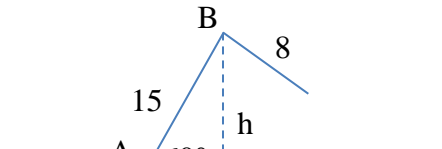
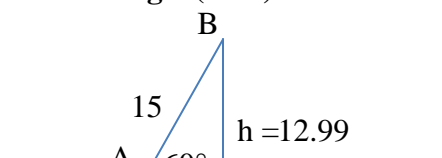
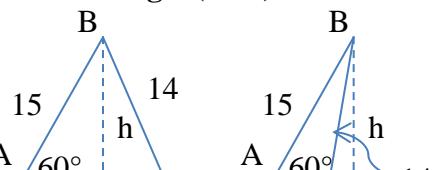
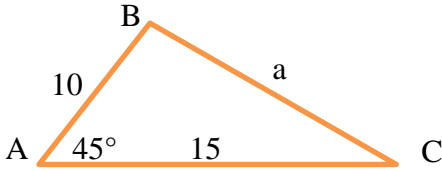
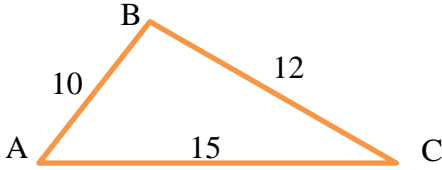


| If You See...  | You Should Think...   |
|--|---|
| <p><b>Angle-Angle-Side (AAS)</b></p>                            | <p><b>Law of Sines (one solution)</b> (note: <math>\angle B = 180^\circ - \angle A - \angle C = 110^\circ</math>)</p> $\frac{\sin C}{c} = \frac{\sin A}{a} \rightarrow \frac{\sin 35^\circ}{10} = \frac{\sin 45^\circ}{a}$ (solve for a)<br>$\frac{\sin C}{c} = \frac{\sin B}{b} \rightarrow \frac{\sin 35^\circ}{10} = \frac{\sin 110^\circ}{b}$ (solve for b)   |
| <p><b>Angle-Side-Angle (ASA)</b></p>                            | <p><b>Law of Sines (one solution)</b> (note: <math>\angle B = 180^\circ - \angle A - \angle C = 110^\circ</math>)</p> $\frac{\sin C}{c} = \frac{\sin B}{b} \rightarrow \frac{\sin 35^\circ}{12} = \frac{\sin 110^\circ}{b}$ (solve for c)<br>$\frac{\sin B}{b} = \frac{\sin A}{a} \rightarrow \frac{\sin 110^\circ}{12} = \frac{\sin 45^\circ}{a}$ (solve for a)  |
| <p><b>Side-Side-Angle (SSA): A obtuse, a &gt; c</b></p>         | <p><b>Law of Sines (one solution)</b><br/>         (note: because <math>a &gt; c</math>, there is only one solution)</p> $\frac{\sin C}{c} = \frac{\sin A}{a} \rightarrow \frac{\sin C}{12} = \frac{\sin 110^\circ}{15}$ (solve for $\angle C$ and then $\angle B$ )<br>$\frac{\sin B}{b} = \frac{\sin A}{a} \rightarrow \frac{\sin B}{b} = \frac{\sin 110^\circ}{15}$ (solve for b)                                |
| <p><b>Side-Side-Angle (SSA): A obtuse, a ≤ c</b></p>           | <p><b>No solution</b></p> <p>There is no solution because side a (length 12) is too short to ever reach side b (which is at least 15 units away). Therefore, no triangle can be constructed.</p>  |
| <p><b>Side-Side-Angle (SSA): A acute a &gt; c &gt; h</b></p>  | <p><b>Law of Sines (one solution)</b><br/>         (note: because <math>a &gt; c</math>, there is only one solution)</p> $\frac{\sin C}{c} = \frac{\sin A}{a} \rightarrow \frac{\sin C}{15} = \frac{\sin 60^\circ}{16}$ (solve for $\angle C$ ,<br>$\angle B = 180^\circ - \angle A - \angle C$ , and then find b using the Law of Sines).  |
| <p><b>Side-Side-Angle (SSA): A acute a &lt; h</b></p>         | <p><b>No solution</b></p> <p>Calculate <math>h = 15\sin 60^\circ</math> using SOHCAHTOA. <math>a = 8 &lt; 12.99 = h</math>. There is no solution because side a is too short (length 8) to ever reach side b (at least 12.99 units away). Therefore, no triangle can be constructed.</p>  |
| <p><b>Side-Side-Angle (SSA): A acute a = h</b></p>            | <p><b>Right Triangle (one solution)</b></p> <p>Calculate <math>h = 15\sin 60^\circ</math>. <math>a = 12.99 = h</math>. There is one solution because side a is perpendicular to side b (right triangle). Therefore, use the Pythagorean Theorem to find side b (<math>15^2 - 12.99^2 = b^2</math>). <math>\angle B = 180^\circ - \angle A - \angle C = 30^\circ</math>.</p>   |
| <p><b>Side-Side-Angle (SSA): A acute c &gt; a &gt; h</b></p>  | <p><b>Law of Sines (2 solutions)</b></p> <p>Calculate <math>h = 15\sin 60^\circ</math>. <math>B = 15 &gt; a = 14 &gt; 12.99 = h</math>. There are two solutions because <math>\sin(\angle C)</math> is positive for two values of <math>\angle C</math> (one acute, one obtuse). Find the two values of <math>\angle B</math>. Then use the Law of Sines for each of the two possible triangles to find side b.</p> |

|   |   |
|---|---|
| <p><b>Side-Angle-Side (SAS)</b></p>  | <p><b>Law of Cosines (one solution)</b></p> $a^2 = b^2 + c^2 - 2bc \cos A = 15^2 + 10^2 - 2(15)(10) \cos 45^\circ$ <p>Then use the Law of Sines to find <math>\angle C</math> and then <math>\angle B = 180^\circ - \angle A - \angle C</math>.</p>   |
| <p><b>Side-Side-Side (SSS)</b></p>   | <p><b>Law of Cosines (one solution)</b></p> $a^2 = b^2 + c^2 - 2bc \cos A \rightarrow 12^2 = 15^2 + 10^2 - 2(15)(10) \cos A$ <p>Solve for <math>\angle A</math>. Then use the Law of Sines to find <math>\angle C</math>, and then <math>\angle B = 180^\circ - \angle A - \angle C</math>.</p> |